Journal of Circuits, Systems, and Computers Vol. 26, No. 7 (2017) 1750106 (16 pages) © World Scientific Publishing Company DOI: 10.1142/S0218126617501067



An Approach to Microcontroller-Based Realization of Boost Converter with Quasi-Sliding Mode Control^{*}

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> Received 30 July 2016 Accepted 7 December 2016 Published 26 January 2017

The paper considers a realization of quasi-sliding mode control for DC–DC boost-type converter on ATmega8 microcontroller. The proposed control law represents a combination of discretetime sliding mode and generalized minimum variance control techniques. The control design is based on input–output converter model and only the sensed output voltage is used for generating control signal. This approach simplifies the practical realization of boost converter since there is no need for current sensors. By introducing an additional discrete-time integrator in control, the converter accuracy in steady-state under load and input voltage variations is enhanced. The experimental prototype is developed and several experiments are conducted to validate the functionalities of the proposed solution. The maximum load and line regulation errors of the proposed converter are 1.55% and 2.9%, respectively.

Keywords: Boost converter; continuous conduction mode; quasi-sliding mode control; generalized minimum variance control; pulse width modulation; digital signal processing.

1. Introduction

The sliding mode (SM) control belongs to the class of nonlinear control known as variable structure control.^{1–3} It forces system state to slide along predefined surface providing system robustness to parameter variations and external disturbances, even invariance⁴ for systems satisfying matching conditions. These SM control properties recommend it for DC–DC converting applications under load variations. However, SM control operates at varying switching frequency causing inductor and transformer core losses, as well as producing some EMI noise issues. This problem can be overcome

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by using a control based on pulse-width-modulation (PWM) fixed-frequency techniques, also known as a duty cycle control,⁵ It has been proven⁶ that the system dynamics with SM controller is equivalent to the system dynamics with PWM controller, i.e., the SM equivalent control^{4,1} u_{eq} is equal to the duty cycle control signal d.

The implementation of PWM techniques in control of DC–DC boost-type converter operating in continuous conduction mode (CCM) may cause the appearance of right-half-plane-zero (RHPZ) in its duty-cycle-to-output-voltage transfer function, obtained on the basis of the state-space average model^{7,8} of converter. This makes the design of boost converter voltage controller more difficult and limits the system bandwidth.⁹ In recent years, several boost converters with PWM-based SM control have been developed. A unified approach to design of PWM-based SM voltage controller for three basic converters (buck, boost and buck-boost) is demonstrated in Ref. 10. The fixed-frequency SM current controller for boost converter is considered in Ref. 11. In order to increase the steady-state accuracy of boost converter, an additional double-integral term of the controlled variables is introduced in the sliding surface equation of indirect SM controllers.¹² Based on the similar state-space model of boost converter as in the previous works,^{10–12} the proportional plus integral (PI) type of switching (sliding) function is introduced in Ref. 13 to cope with load variations. Moreover, the switching function parameter is tuned as per a load, resulting in adaptive unlike conventional SM control. The fast terminal SM control, having a nonlinear switching function to guarantee finite-time convergence to sliding surface, is implemented in the output voltage control of boost converter.¹⁴ The proposed control scheme combines finite-time and exponent convergent properties in design of switching function, in order to improve the convergence performance if the system state is far from the equilibrium point.

Boost converters are widely used as power stages in renewable energy resources such as photovoltaic (PV) systems. The connection of these systems to a main DC bus via power converters enables high maximum power point tracking (MPPT). Thanks to the fact that the input impedance of boost converter can be tuned by duty cycle, i.e., it can be considered as an adjustable loss-free resistor (LFR), the operating point of PV system can be changed in order to maximize the output power. An overview of MPPT techniques for PV power systems is presented in Ref. 15. Many MPPT methods do not take into account the system uncertainties and are not robust to them. To cope with parameter perturbation, MPPT algorithms with SM control are proposed for eliminating the perturbation effects.^{16,17} In Ref. 18 MPP curve is approximated, taking into account not only the voltage and current on the PV panel, but also the temperature. This linear approximation is used then to form a switching function of SM controller. The impedance matching can be also obtained by the cascade connection of two boost converters driven by SM controllers based on LFR concept.¹⁹

The fixed switching frequency of SM control can be attained by using discretetime SM controllers.^{20–22} However, the discretization process of SM control causes the quasi-sliding motion²³ in the vicinity of sliding surface and produces an undesirable chattering. The latter phenomenon is also present in boost converters with PWM-based continuous-time SM control techniques. It can be suppressed by using the boundary layer approach,¹⁷ the chattering-free^{14,16} control methods or, recently, the tensor product model²⁴ for sliding surface design.²⁵

One of the first approaches in design of discrete-time SM-like controller is considered in Ref. 26 for the control of DC–DC buck converter. The control algorithm is implemented as a fuzzy logic controller with sliding mode-like characteristics. Discrete-time SM controllers for boost converter^{27,28} can be designed based on its statespace average model, which is the nonminimum phase system if the output voltage is directly controlled. Therefore, the indirect method is used that controls the inductor current, whose reference signal is selected such that a desired output voltage is obtained. The choice of inductor current, as an output, results in minimum phase system, but the problem of output voltage convergence to its reference signal arises. In Ref. 27, the design of discrete-time SM control with reference model is presented. The cascade regulation scheme, consisting of the inner inductor current loop with discrete-time SM control and the outer one being composed of a discrete-time PI controller for output voltage regulation, is considered in Ref. 28. Another approach to modeling of boost converter,^{29,30} using discrete Lagrange–Euler equations, results also in nonminimum phase system. The main difficulty to stabilize the unstable inductor current variable and to provide an output voltage that tracks a desired reference signal is addressed in these papers. Due to unstable zero dynamics of statespace average model, the implementation of discrete-time SM control using stable system center³¹ in direct control of the output voltage may be considered as a promising solution to this problem.

All previous control design techniques are based on the state-space model representation of boost converter and, therefore, the measuring of inductor current is mandatory. In this paper, we present a discrete-time SM control, designed by using the input-output model of boost converter in the form of a discrete-time transfer function, which eliminates the need for additional current sensor. The proposed quasi-sliding mode (QSM) control represents the combination of generalized minimum variance (GMV) and discrete-time SM control techniques.^{32,33} GMV control is suggested herein to cope with RHPZ of duty-cycle-to-output-voltage transfer function and to enable the controller design based only on converter output voltage measuring. In order to alleviate chattering and achieve better converter accuracy, the discrete-time SM control component is filtered through discrete-time integrator.³² The theoretical background of the proposed control for the boost converter is given in Ref. 34, based on contributions presented in Ref. 33 and partially in Ref. 32. However, due to parameter variations, some additional stability issues are considered in this paper, extending the theoretical results in that way. Similar QSM controller is implemented in voltage control of buck converter.³⁵ As the buck converter represents

a minimum phase system, the discrete-time SM control is combined with the minimum variance (MV) control.

Traditionally, digital signal processors are used to implement controllers for power converters. In recent years, some research efforts are dedicated to design of low-cost solutions for the voltage control of boost converter. In Ref. 36, the slidingmode hysteretic control algorithm, based on state-space model, is realized on lowcost memory hardware. The sliding surface is derived in advance and stored in memory lookup table, whose output drives a boost converter power switch. The continuous-time SM control, designed by using state-space average model, is digitally implemented using low-cost dsPIC30F4013 microcontroller with small computing power.³⁷ The selection of sliding surface provides the current mode controller, making the inductor current a function of the output voltage. In this paper, we demonstrate how the proposed QSM control for boost converter can be realized on widely used ATmega8 microcontroller. It is shown that this control is simple enough to be easily implemented on standard 8-bit microcontrollers, but at the expense of little lower accuracy and slower dynamical response. Moreover, the proposed boost converter realization gives satisfactory experimental results, indicating that better results can be expected if digital signal processor is used.

The paper is organized as follows. In Sec. 2, the modeling of boost converter is considered. The brief design procedure of proposed QSM control algorithm is given in Sec. 3. The experimental setup is presented and the experimental results are discussed in Sec. 4. Section 5 contains some concluding remarks.

2. Boost Converter Modeling

Mathematical models of the boost converter provide the pathway to various control strategies discussed in literature. In this paper, the model of boost converter is given in the form of discrete-time transfer function, derived from the state-space model.¹⁰ The schematic diagram of boost converter with the proposed QSM controller is shown in Fig. 1. Herein, C_k , L and R_L represent the capacitance, inductance and load resistance of the converter, respectively; i_c , i_L and i_{out} are the capacitor, inductor and output (load) currents, respectively; V_{ref} , v_{in} and v_{out} denote the reference, input, and output voltages, respectively; β denotes sensor gain, whereas u representing the signal driving the power switch S_w . The boost converter operating in CCM is considered in modeling process. By taking the output voltage and its time-derivative for the state coordinates ($x_1 = v_{out}, x_2 = dv_{out}/dt$), the linearized small-signal state-space model of boost converter in continuous-time domain can be written in the following form¹⁰:

$$\dot{x}(t) = \begin{bmatrix} 0 & 1 \\ 0 & -\frac{1}{R_L C_k} \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ \frac{V_{\rm in} - V_{\rm out}}{L C_k} \end{bmatrix} u(t) , \qquad (1)$$
$$y(t) = \begin{bmatrix} \beta & 0 \end{bmatrix} x(t) ,$$



Fig. 1. Boost converter with QSM controller.

where $V_{\rm in}$ and $V_{\rm out}$ are the nominal values of boost converter input and output voltages.

The transfer function of boost converter can be derived directly from Eq. (1) as

$$W_{\text{boost}}(s) = \frac{Y(s)}{U(s)} = \frac{\frac{\beta(V_{\text{in}} - V_{\text{out}})}{LC}}{s^2 + \frac{1}{R_L C}s}.$$
 (2)

Under the assumption that control signal is constant during the sampling period T, u(t) = u(kT), kT < t < (k+1)T, the input-output model of boost converter in z-domain is given by

$$y(k) = \frac{z^{-1}B(z^{-1})}{A(z^{-1})}u(k), \qquad (3)$$

where z^{-1} is the unit delay, i.e., $z^{-1}=e^{-{}^{sT}},\,s$ denotes a complex variable, $\bullet(k)=\bullet(kT)$ and

$$A(z^{-1}) = A_n(z^{-1}) + \Delta A(z^{-1}),$$

$$B(z^{-1}) = B_n(z^{-1}) + \Delta B(z^{-1}),$$
(4)

 $A_n(z^{-1}), B_n(z^{-1}), \Delta A(z^{-1})$ and $\Delta B(z^{-1})$ represent the polynomials with nominal and perturbed values of boost converter parameters, respectively.

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3. QSM Control Law

The main aim of control design is to maintain the sensed output voltage $y(k) = \beta v_{\text{out}}(k)$ as stable, constant and equal to some reference voltage $V_r(k) = V_{\text{ref}}$, despite the variations of load resistance R_L and input voltage v_{in} . In order to achieve the design task, QSM control algorithm^{32,33} is used to control boost converter. It is defined by

$$u(k) = -\frac{F(z^{-1})y(k) - C(z^{-1})V_r(k+1) + \frac{\alpha^T}{1 - z^{-1}}\operatorname{sgn}(s(k))}{E(z^{-1})B_n(z^{-1}) + Q(z^{-1})},$$
(5)

where s(k) represents the switching function given by

$$s(k+1) = C(z^{-1})(y(k+1) - V_r(k+1)) + Q(z^{-1})u(k),$$
(6)

 $C(z^{-1})$ is a polynomial with all zeros inside the unit disk of z-plane, and Q(1) = 0. $E(z^{-1})$ and $F(z^{-1})$ are solutions of the so-called Diophantine equation:

$$C(z^{-1}) = E(z^{-1})A_n(z^{-1}) + z^{-1}F(z^{-1}),$$
(7)

s(k) = 0 is an equation of sliding surface in general case. The closed-loop dynamics is directly derived from Eqs. (3) and (6) in the form of ³²:

$$y(k) = \frac{B(z^{-1})(C(z^{-1})V_r(k) + s(k))}{B(z^{-1})C(z^{-1}) + A(z^{-1})Q(z^{-1})},$$
(8)

It is obvious from Eq. (8) that, in order to guarantee the system stability, all roots of the equation $B(z^{-1})C(z^{-1}) + A(z^{-1})Q(z^{-1}) = 0$ should be inside the unit disk in the z-plane, and the pairs $(B(z^{-1}), Q(z^{-1})), (C(z^{-1}), A(z^{-1}))$ and $(C(z^{-1}), Q(z^{-1}))$ should not have common zeroes outside this disk. The system steady-state accuracy can be obtained from Eq. (8) for z = 1 and Q(1) = 0 as

$$y(\infty) = V_r(\infty) + \frac{1}{C(1)}s(\infty).$$
(9)

Substituting Eq. (5) in Eq. (3), taking into account Eqs. (4), (6) and (7), one gets

$$B(z^{-1})s(k+1) = -\frac{\alpha T B(z^{-1})\operatorname{sgn}(s(k))}{1-z^{-1}} + E(z^{-1})P(z^{-1})y(k+1), \quad (10)$$

where $P(z^{-1}) = A_n(z^{-1})\Delta B(z^{-1}) - B_n(z^{-1})\Delta A(z^{-1})$. Replacing y(k+1) in Eq. (10) by Eq. (8), having in mind that $V_r(k+1) = V_r(k) = V_{ref} = \text{const.}$, gives:

$$\Delta s(k+1) = -\frac{B(z^{-1})C(z^{-1}) + A(z^{-1})Q(z^{-1})}{B(z^{-1})C(z^{-1}) + A(z^{-1})Q(z^{-1}) - E(z^{-1})P(z^{-1})} \alpha T \operatorname{sgn}(s(k)), \quad (11)$$

where $\Delta s(k+1) = s(k+1) - s(k)$ is bounded if all roots of the equation $B(z^{-1})C(z^{-1}) + A(z^{-1})Q(z^{-1}) - E(z^{-1})P(z^{-1}) = 0$ are inside the unit disk in the z-plane.

The latter is accomplished by the appropriate selection of the polynomials $C(z^{-1})$ and $Q(z^{-1})$. Finally, the switching function dynamics is defined as

$$s(k+1) = s(k) - \alpha T \operatorname{sgn}(s(k)) + l(k+1), \qquad (12)$$

with

$$l(k) = \frac{E(z^{-1})P(z^{-1})}{B(z^{-1})C(z^{-1}) + A(z^{-1})Q(z^{-1})} \Delta s(k), \qquad (13)$$

including all parameter perturbations and, obviously, $|l(k)| \leq \Lambda$, where Λ is a positive real constant. If $\alpha > \Lambda/T$, a quasi-sliding motion is established in Δ -vicinity of s(k) = 0, i.e., $|s(k)| \leq \Delta$ is always satisfied, where Δ is a function of αT . The proof of this statement is beyond the scope of this paper, and can be found in Ref. 35.

4. Experimental Prototype and Results

The verification of proposed boost converter is presented in this section. The developed experimental prototype is depicted in Fig. 2, whereas the scheme of microcontroller based boost converter is given in Fig. 3. Table 1 contains the nominal values of converter parameters. With T = 1 ms, the discrete-time model (Eq. (3)) is defined by $A(z^{-1}) = 1 - 1.9802z^{-1} + 0.9802z^{-2}$ and $B(z^{-1}) = 1.3515 - 1.3425z^{-1}$. Then, the parameters of QSM controller are selected and calculated as: $C(z^{-1}) =$ $1 - 1.067z^{-1} + 0.2846z^{-2}$, $Q(z^{-1}) = 0.05(1 - z^{-1})$, $E(z^{-1}) = 1$, $F(z^{-1}) = 0.9132 0.6956z^{-1}$ and $\alpha = 10$.



Fig. 2. Experimental prototype of the proposed boost converter.



Fig. 3. Scheme of boost converter realization with ATmega8 microcontroller.

Description	Parameter	Nominal Value
Input voltage	$V_{ m in}$	$12\mathrm{V}$
Desired output voltage	$V_{\rm out}$	$24\mathrm{V}$
Capacitance	C_k	$1,\!470\mu\mathrm{F}$
Inductance	L	$330\mu\mathrm{H}$
PWM frequency	$f_{ m pwm}$	$7.874\mathrm{kHz}$
Sampling period	T	$1\mathrm{ms}$
Minimum load resistance	R_{L_\min}	22.67Ω
Maximum load resistance	R_{L_\max}	68Ω

Table 1. Boost converter parameter values.

QSM control algorithm is realized by using 8-bit microcontroller ATmega8.³⁸ The sensed output voltage is fed into its 10-bit A/D converter. PWM is also incorporated in microcontroller with the switching frequency $f_{\rm pwm} = 7.874$ kHz. Thanks to such choice of $f_{\rm pwm}$, the influence of RHPZ in duty-cycle-to-output-voltage transfer functions is significantly suppressed but at the cost of lower bandwidth.⁷



Fig. 4. Experimental waveforms of $v_{\rm out}$ (panels (a)–(c)) and $i_{\rm out}$ (panel (d)) of the boost converter with QSM control, alternating between load resistances 68 Ω and 34 Ω and operating at (a) $V_{\rm in} = 10.5$ V, (b) $V_{\rm in} = 12$ V and (c) $V_{\rm in} = 13.5$ V.



Fig. 4. (Continued)



Fig. 5. Experimental waveforms of $v_{\rm out}$ (panels (a)–(c)) and $i_{\rm out}$ (panel (d)) of the boost converter with QSM control, alternating between load resistances 34Ω and 22.67Ω and operating at (a) $V_{\rm in} = 10.5$ V, (b) $V_{\rm in} = 12$ V and (c) $V_{\rm in} = 13.5$ V.



Fig. 5. (Continued)

In order to analyze load and line regulation properties of the realized microcontroller based boost converter with QSM control, the step load changes from $R_L = 68 \Omega$ to $R_L = 34 \Omega$, from $R_L = 34 \Omega$ to $R_L = 22.67 \Omega$ and from $R_L = 68 \Omega$ to $R_L = 22.67 \Omega$ are applied at three different input voltage values: minimum $(V_{\rm in} = 10.5 \text{ V})$, nominal $(V_{\rm in} = 12 \text{ V})$ and maximum $(V_{\rm in} = 13.5 \text{ V})$. The experimental

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results in the form of output voltage v_{out} and current i_{out} waveforms are presented in Figs. (4)–(6).

According to Table 2, maximum load regulation error occurs at $V_{\rm in} = 10.5$ V with deviation of 1.55% from $V_{\rm out}$ at nominal condition. On the other hand, the maximum line regulation error is at maximum load ($R_L = 22.67 \Omega$) with deviation of 2.9% from



Fig. 6. Experimental waveforms of $v_{\rm out}$ (panels (a)–(c)) and $i_{\rm out}$ (panel (d)) of the boost converter with QSM control, alternating between load resistances 68 Ω and 22.67 Ω and operating at (a) $V_{\rm in} = 10.5$ V, (b) $V_{\rm in} = 12$ V and (c) $V_{\rm in} = 13.5$ V.



Table 2. Load regulation property ($V_{\text{out (nominal condition)}} = 23.9 \text{ V}$ at $V_{\text{in}} = 12 \text{ V}$ and $R_{\text{L-min}} = 22.67 \Omega$).

$V_{ m in}$	$\Delta V_{\mathrm{out}} = V_{\mathrm{out}_{(68\Omega)}} - V_{\mathrm{out}_{(22.67\Omega)}}$	$\frac{\Delta V_{\rm out}}{V_{\rm out(nominal \ condition)}} \times 100\%$
10.5 V	0.37 V	1.55% of $V_{\text{out (nominal condition)}}$
12 V	$0.32 \mathrm{V}$	1.32% of $V_{ m out\ (nominal\ condition)}$
13.5 V	0.21 V	0.89% of $V_{\rm out\ (nominal\ condition)}$

Table 3. Line regulation property ($V_{\text{out (nominal condition)}} = 23.9 \text{ V}$ at $V_{\text{in}} = 12 \text{ V}$ and $R_{\text{L}_\text{min}} = 22.67 \Omega$).

Loading condition	$\Delta V_{\rm out} = V_{\rm out_{(V\rm in=13.5V)}} - V_{\rm out_{(V\rm in=10.5V)}}$	$\frac{\Delta V_{\rm out}}{V_{\rm out(nominal \ condition)}} \times 100\%$
$R_{\rm L_max} = 68\Omega$	$0.4\mathrm{V}$	1.67% of $V_{\text{out (nominal condition)}}$
$R_{\rm L_medium} = 34\Omega$	$0.3\mathrm{V}$	1.25% of $V_{\rm out\ (nominal\ condition)}$
$R_{ m L_min} = 22.67\Omega$	$0.7\mathrm{V}$	2.9 % of $V_{\rm out\ (nominal\ condition)}$

 V_{out} at nominal condition (see Table 3). It is worth noting that the load and line regulation properties depend largely on microcontroller's A/D converter and PWM resolution, as well as on the choice of QSM controller parameters $C(z^{-1})$, α and T. Theoretically, according to Eq. (9), the converter steady-state error should be approximately 400 mV. Therefore, a better accuracy may be expected if a faster microcontroller with better A/D converter and PWM resolution is used.

5. Conclusion

In this paper, the quasi-sliding mode control for DC–DC boost-type converter is discussed, and its realization on 8-bit ATmega8 microcontroller is presented.

The proposed control is a combination of discrete-time sliding mode control and generalized minimum variance control, and can be implemented by measuring only converter output voltage without the need for additional current sensors. The experimental prototype is developed and several tests are carried out. The experimental results demonstrate good regulation performances under load and input voltage variations, in spite of low resolution of A/D converter and PWM. Better results may be expected with faster digital signal processors. It can be concluded that the proposed boost converter with quasi-sliding mode control is feasible by using standard 8-bit microcontrollers.

Acknowledgments

This paper was realized as a part of the Projects III 43007 and TR 35005 financed by the Ministry of Education, Science and Technological Development of the Republic of Serbia.

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