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Asymptotic Solution of Singularly Pertubeted **Problems with Quadratic Small Parameter**

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bstract

In this paper we study singularly pertarbed with initial problem of the system with two linear ry differential expositions, each of which contains small parameter in its derivative and quadratic e same small parameter in one of them. A uniform asymptotic expansion is constructed on a time stary al solution of the problem, obtained formulas for the terms of internal expansion, they allow us to ad them only through algebraic operations, finally we give examples which related with our subject.

Leywords: Differential equations, asymptotic, singularly perturbed , boundary function, small

الخلاصة

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See 1

في هذا الحث عربينا سالة الاستقراب السفرة بالتروط الاشائية تطالر من من السعاد لات القاضيفة العادية الخطية، كا منها يعتري على معلمة مسجرة في مشافاتها والتربيعية من على المعلمة المسجرة في واحد منهم. ثم يتاد توسيع ستنقر التطري، متن فرا من الزين لما السالة. حسلنا على سيمة من المتود تتوسيع الغارجي، قتى تسبح لنا بايجادها من خال السليات الجبرية. وأخبرا المنا أمثلة التي تلعلل بموضوعنا

التلمان الملاحية الدمادلات القاصلية التاريب التناطري ، الاسطراب السترد، الدالة الحترجية، المعلمة المسعيرد، المعطمة الاساس،

Mathematics Subject Classification : 34E15

The subject of differential equations with small parameters high derivatives I.Introduction: arise in the modeling and study of physical, biological, chemical phenomena and processes. This kind of equations are also found in automatic control theories. nonlinear oscillations, in gas dynamics, in the description of gyroscopic systems. These equations are called singularly perturbed. Their feature is that the order of the degenerate equation resulting from the initial with zero values of the parameters, lower than the order of the original equations, as a consequence, the solution of the degenerate equation can not satisfy all the conditions specified for the initial equation.

The problem as the formula:

 $\frac{dy}{dx} = f(x, y) \quad , \quad y(x_0) = y_0$

Primarilies of the theorey of singular perturbitions are the works of Is called Cauchy problem with initial point se-[Tikhonov ,1948,1950,1952], in which a general statement of the problem is given the Cuachy problem of systems of nonlinear ordinary differential equations with small purameeters for derivatives and the lamiting transition from the solution for the original problem to the solution of the degentrate problem when the parameters tend to zero

Asymptotic solution of singularly pertubeted problems with quadratic small parameter

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Abstract:

In this paper we study singularly perturbed with initial problem of the system with two linear ordinary differential equations, each of which contains small parameter in its derivative and quadratic the same small parameter in one of them. A uniform asymptotic expansion is constructed on a time interval solution of the problem. obtained formulas for the terms of internal expansion, they allow us to find them only through algebraic operations, finally we give examples which related with our subject.

Keywords: Differential equations, asymptotic, singularly perturbed, boundary function, small parameter, direct scheme.

Mathematics subject classification : 34E15

I.Introduction:

The subject of differential equations with small parameeters high derivatives arise in the modeling and study of physical, biological, chemical phenomena and processes. This kind of equations are also found in automatic control theories, nonlinear oscillations, in gas dynamics, in the description of gyroscopic systems. These equations are called singularly perturbed. Their feature is that the order of the degenerate equation resulting from the initial with zero values of the parameeters, lower than the order of the original equations, as a consequence, the solution of the degenerate equation can not satisfy all the conditions specified for the initial equation. The problem as the formula:

$$\frac{dy}{dx} = f(x, y) \quad , \quad y(x_0) = y_0$$

Is called Cauchy problem with initial point x_0 .

Primarilies of the theorey of singular perturbtions are the works of [A.N. Tikhonov ,1948,1950,1952], in which a general statement of the problem is given the Cuachy problem of systems of nonlinear ordinary differential equations with

small parameters for derivatives and the limiting transition from the solution for the orignal problem to the solution of the degenrate problem when the parameters tend to zero.

Construction of approximation solutions of singularly perturbed problems is carried out in many ways, both numerically and asymptotically. The most widely accepted among the asymptotic methods are the method boundary functions [A.B Vasil'eva, 1969, 1959, 1963, 1973, 1990, 1962].

In this paper we consider the following singularly perturbed problem. The Cauchy problem of a system with two ordinary differential equations with quadratic small parameeters for derivatives. The behavior of the solution for the problem at a finite time interval is studied. The novelty of the problems of this study is that small parameeter that is in the two equations of the system each for its derivative, tend to zero independently of each other. In this way, we are talking about the construction of an asymptotics of the solution that is uniformly suitable for any relations between small parameeters.

II.view Problem:

Consder the system:

Such that a(t),b(t),c(t),d(t), are infinite differential functions on [0,T], satisfy the conditions a(t)<0, d(t)<0, $D = \begin{vmatrix} a & b \\ c & d \end{vmatrix} > 0$, for every $t \in [0,T]$.

Where $\varepsilon > 0$ is small parameter.

III.The constraction of formula for solution of the problem:

The asymptotic expansion for the solution of problem (1),(2) will be constructed as type:

$$x(t,\varepsilon) = \bar{x}(t,\varepsilon) + \pi_x(\tau,\varepsilon)$$

$$y(t,\varepsilon) = \bar{y}(t,\varepsilon) + \pi_y(\tau,\varepsilon)$$
......(3)

$$\bar{x}(t,\varepsilon) = \sum_{i,j=0}^{\infty} \varepsilon^{i+2j} \, \bar{x}_{i,j}(t) \, ,$$

 $\bar{y}(t,\varepsilon) = \sum_{i,j=0}^{\infty} \varepsilon^{i+2j} \, \bar{y}_{i,j}(t), \ \tau = \frac{t}{\varepsilon^3}$

Now by substituting the expansion (3) in the equations 1-2 and equating coefficients which the same power of ε we can determine the cofficients of series (3).

In partcular, the system for finding $x_{0,0}$, $y_{0,0}$ coincides with a degenrate system of the system (1) (at ε =0).

The remaining coefficients of the expansion (3) are found from systems of linear algebraic equations of the form:

$$A(t)W_{m,n}(t) = T_{m,n}(t) \dots \dots \dots (4)$$

Where

$$A(t) = \begin{bmatrix} a(t) & b(t) \\ c(t) & d(t) \end{bmatrix}, W_{m,n}(t) = \begin{bmatrix} x_{m,n}(t) \\ y_{m,n}(t) \end{bmatrix} \dots \dots (5)$$

A vector valued unctions $T_{m,n}$ can be expressed in terms of $W_{i,j}$, (i + j < n + m). We note that the systems (4) have an uniquely solution, because from the condition (2) we have the relation det $(A) \neq 0$, $\forall t \in [0,T]$.

Further, we expand the functions a(t),b(t),c(t),d(t) in power series in neighborhoods of the point t=0 with coeffcients a_i, b_i, c_i, d_i [i=0,1,2,...], respectively and new variable τ .

Without loss of generality view of condition (D > 0) we assume that $a_0=d_0=-1$. The internal expansion π_x , π_y can be written by the following type:

$$\pi_{\chi}(\tau,\varepsilon) = \sum_{i,j=0}^{\infty} \varepsilon^{i+2j} \pi_{\chi}^{ij}(\tau), \\ \pi_{y}(\tau,\varepsilon) = \sum_{i,j=0}^{\infty} \varepsilon^{i+2j} \pi_{y}^{ij}(\tau) \dots \dots (6)$$

Such that:

 π_x^{ij}, π_y^{ij} , are a boundary functions in a neighborhoods of t=0 and it satisfies the following equality :

$$\left\|\pi_g^i(\tau)\right\| \le c e^{-\omega \tau_i}, \quad g = x, y \dots \dots \dots \dots (7)$$

Where c, ω are positive constants.

Substituting equation (6) in equation (1) we obtain :

$$\varepsilon^{-2} \sum_{i,j=0}^{\infty} \varepsilon^{i+2j} \frac{d\pi_x^{ij}}{d\tau} = \left(\sum_{i=0}^{\infty} a_i \tau^i \varepsilon^{3i}\right) \sum_{i,j=0}^{\infty} \varepsilon^{i+2j} \pi_x^{ij} + \left(\sum_{i=0}^{\infty} b_i \tau^i \varepsilon^{3i}\right) \sum_{i,j=0}^{\infty} \varepsilon^{i+2j} \pi_y^{ij}$$
$$\varepsilon^{-1} \sum_{i,j=0}^{\infty} \varepsilon^{i+2j} \frac{d\pi_y^{ij}}{d\tau} = \left(\sum_{i=0}^{\infty} c_i \tau^i \varepsilon^{3i}\right) \sum_{i,j=0}^{\infty} \varepsilon^{i+2j} \pi_x^{ij} + \left(\sum_{i=0}^{\infty} d_i \tau^i \varepsilon^{3i}\right) \sum_{i,j=0}^{\infty} \varepsilon^{i+2j} \pi_y^{ij}$$
We denote $\zeta_{m,n}(.) = \begin{bmatrix} \pi_x^{mn} \\ \pi_y^{mn} \end{bmatrix} \dots \dots (8)$

We will seek $\zeta_{m,n}(\tau,\varepsilon)$ by solving the following systems of differential equations with constant coefficients:

$$\frac{d}{d\tau}\zeta_{m,n} = A_0(\varepsilon)\zeta_{m,n}(\tau,\varepsilon) + S_{m,n}(\tau,\varepsilon), m, n = 0, 1, \dots \dots (9)$$

Such that:

$$S_{m,n}(\tau,\varepsilon) = \sum_{i=0}^{\min\{m,n\}} \tau^i A_i , A_i = \begin{bmatrix} \varepsilon^2 a_i & \varepsilon^2 b_i \\ \varepsilon c_i & \varepsilon d_i \end{bmatrix}$$

With the conditions:

$$\zeta_{0,0}(0,\varepsilon) = W_0 - W_{0,0}(0) \dots \dots \dots (10)$$

$$\zeta_{m,n}(0,\varepsilon) = -W_{m,n}(0) \dots \dots \dots (11)$$

$$W_0 = \binom{x_0}{y_0}$$

Thus the formula of construction of the series (3) is complete to be proved that these series are inded an asymptotic expansion solution of the problem on the closed interval [0,T].

IV. Estimate of e terms of internal expansion:

4.1.Definition:

Let λ_1, λ_2 are eigenvalues of matrix $A_0(\varepsilon)$ then:

$$\lambda_i = \frac{-\varepsilon - \varepsilon^2 \pm \sqrt{(\varepsilon + \varepsilon^2)^2 - 4\varepsilon^3 D_0}}{2}$$

$$\lambda_{i} = \frac{-\varepsilon - \varepsilon^{2} \pm \sqrt{(\varepsilon - \varepsilon^{2})^{2} + 4\varepsilon^{3}b_{0}c_{0}}}{2}$$
$$\lambda_{i} = \frac{-\varepsilon - \varepsilon^{2} \pm \varepsilon\sqrt{(1 - \varepsilon)^{2} + 4\varepsilon b_{0}c_{0}}}{2} , i = 1,2$$

Where $D_0 = 1 - b_0 c_0 > 0$

Depending on the values of b_0, c_0 in the matrix $A_0(\varepsilon)$ in definition 4.1, we can disscaus the cases:

1- λ_1, λ_2 are real ,different with note that $\lambda_2 < \lambda_1 < 0$.

In this case we realize its with the following relations:

$$\begin{split} &i - b_0 c_0 > 0 \ , \forall \ \varepsilon > 0. \\ &ii - b_0 c_0 = 0 \ and \ \varepsilon \neq 0 \ , \varepsilon \neq 1 \\ &2 - \lambda_1 = \ \lambda_2 \in R. \end{split}$$

This case is realized at the conditions: $b_0 c_0 = 0$ and $\varepsilon = 0$, 1

 $3-\lambda_1, \lambda_2$ are complex with its conjugate.

This case is hold e condition: $Re(\lambda_i) = \frac{-\varepsilon(1+\varepsilon)}{2} < \frac{-\varepsilon^2}{1+\varepsilon}$

Since :

$$\begin{aligned} |\lambda_{2}| &= \frac{\varepsilon + \varepsilon^{2} + \varepsilon\sqrt{(1+\varepsilon)^{2} - 4\varepsilon D_{0}}}{2} > \frac{\varepsilon(1+\varepsilon)}{2} > |\lambda_{1}| \\ &= \frac{\varepsilon + \varepsilon^{2} - \varepsilon\sqrt{(1+\varepsilon)^{2} - 4\varepsilon D_{0}}}{2} = \frac{2\varepsilon^{3} D_{0}}{\varepsilon + \varepsilon^{2} + \varepsilon\sqrt{(1+\varepsilon)^{2} - 4\varepsilon D_{0}}} \\ &> D_{0} \frac{\varepsilon^{3}}{\varepsilon + \varepsilon^{2}} = D_{0} \rho \dots \dots \dots \dots (12) \\ &\rho = \frac{\varepsilon^{3}}{\varepsilon + \varepsilon^{2}} = \frac{\varepsilon^{2}}{1+\varepsilon} \dots \dots (13) \end{aligned}$$

4.2.Proposition:

The exponesial matrix $e^{A_0 \tau}$ satisfies the estimate:

$$\|e^{A_0\tau}\| \leq C_0 e^{-(k\rho(\varepsilon)\tau)}$$
 , $\tau \geq 0$

Such that $C_{0,k}$ are positive constants, it does not depended on τ, ε

Proof:

By using [Lappo-Danilevsky I.A., 1957, p.49) we have :

$$e^{A_0\tau} = e^{\lambda_2\tau}I + \frac{e^{\lambda_1\tau} - e^{\lambda_2\tau}}{\lambda_1 - \lambda_2} (A_0 - \lambda_2 I) \dots \dots \dots (14)$$
$$\|A_0 - \lambda_2 I\| \le k\varepsilon (1 + \varepsilon) \dots \dots \dots \dots (15)$$

In case(1) of estimate we have the inqualities:

By definition of λ_i and equation(15) we obtain:

$$\lambda_1 - \lambda_2 = \varepsilon \sqrt{(1 - \varepsilon)^2 + 4\varepsilon b_0 c_0}$$

Thus:

$$\frac{\|A_0 - \lambda_2 I\|}{\lambda_1 - \lambda_2} \le k \frac{\varepsilon (1 + \varepsilon)}{\varepsilon \sqrt{(1 - \varepsilon)^2 + 4\varepsilon b_0 c_0}} = k \frac{(1 + \varepsilon)}{\sqrt{(1 - \varepsilon)^2 + 4\varepsilon b_0 c_0}} \le k_{1.....}$$
(17)

Now we note :

$$\frac{e^{\lambda_{1}\tau} - e^{\lambda_{2}\tau}}{\lambda_{1} - \lambda_{2}} = \tau \int_{0}^{1} e^{(\lambda_{2}\tau + \theta(\lambda_{1}\tau - \lambda_{2}\tau))} d\theta$$
$$= \tau \int_{0}^{\frac{1}{2}} e^{(\lambda_{2}\tau + \theta(\lambda_{1}\tau - \lambda_{2}\tau))} d\theta + \tau \int_{\frac{1}{2}}^{1} e^{(\lambda_{2}\tau + \theta(\lambda_{1}\tau - \lambda_{2}\tau))} d\theta$$
$$\leq \tau e^{\frac{\lambda_{2}\tau}{2}} \int_{0}^{\frac{1}{2}} e^{\theta\lambda_{1}\tau} d\theta + \tau e^{\frac{\lambda_{1}\tau}{2}} \int_{\frac{1}{2}}^{1} e^{\theta\lambda_{2}\tau} d\theta$$
$$\leq \frac{k_{2}}{|\lambda_{2}|} \left[e^{\frac{\lambda_{2}\tau}{4}} + e^{\frac{\lambda_{1}\tau}{2}} \right] \dots \dots \dots \dots (18)$$

Now by (17) and (18) and by cases (1),(2) we have the eigenvalues of matrix A₀ satisfy $Re\lambda_i \leq -\lambda$, $\lambda > 0$ and thus obtain:

$$\|e^{A_0\tau}\| \le C \frac{\|A_0\|}{\lambda} e^{-\frac{\lambda\tau}{2}}, \tau \ge 0$$
$$Re(\lambda_i) = \frac{-\varepsilon(1+\varepsilon)}{2}$$

Hence

$$\|e^{A_0 \tau}\| \leq C_0 e^{-(k \rho(\varepsilon) \tau)}$$
 , $\tau \geq 0$

4.3.Example:

$$\varepsilon \frac{dx}{dt} = x - y, \varepsilon^2 \frac{dy}{dt} = x + y \dots \dots \dots (19)$$

 $x(0) = x_0, y(0) = y_0 \dots \dots \dots \dots (20)$

The exact solution of equation (19),(20) have a type:

$$x(t,\varepsilon) = (x_0\varepsilon^2 - y_0\varepsilon)(\varepsilon^2 + \varepsilon) + (x_0 - y_0)\left(\frac{\varepsilon}{\varepsilon + \varepsilon^2}\right)e^{-\frac{\varepsilon + \varepsilon^2}{\varepsilon^3}t}$$
$$y(t,\varepsilon) = (x_0\varepsilon^2 - y_0\varepsilon)(\varepsilon^2 + \varepsilon) - (x_0 - y_0)\left(\frac{\varepsilon^2}{\varepsilon + \varepsilon^2}\right)e^{-\frac{\varepsilon + \varepsilon^2}{\varepsilon^3}t}$$

These formulas show that in the case when the parameters ε tend to zero, it is not possible to represent the solution of the problem in the form of a series of the power of the parameters with coefficients that depend on the new scale $\frac{\varepsilon + \varepsilon^2}{\varepsilon^3}$ because the factor $\frac{\varepsilon + \varepsilon^2}{\varepsilon^3}$ does not decompose under exponentials in a power series of ε .

In calculating the asymptotic solution, we find that the external expansion is trivial and internal expansion contains only the principal terms:

 $\pi_x(\tau,\varepsilon) = \pi_x^{00}(\tau), \pi_y(\tau,\varepsilon) = \pi_y^{00}(\tau)$, that means the internal solution identically coinciding with the exact solution by substitution $\tau = \frac{t}{\varepsilon^3}$.

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الحل التناظري لمسائل الاضطراب المنفردة بمعلمة صغيرة تربيعية

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<u>الملخص:</u>

في هذا البحث درسنا مسألة الاضطراب المنفرد بالشروط الابتدائية لنظام من من المعادلات النفاضلية العادية الخطية، كل منها يحتوي على معلمة صغيرة في مشتقاتها والتربيعية من نفس المعلمة الصغيرة في واحد منهم. تم بناء توسيع منتظم تناظري على فترة من الزمن لحل المسألة. حصلنا على صيغة من الحدود للتوسيع الخارجي التي تسمح لنا بايجادها من خلال العمليات الجبرية، وأخيرا قدمنا أمثلة التي تتعلق بموضوعنا.

<u>الكلمات المفتاحية</u>:المعادلات التفاضلية،التقريب التناظري ، الاضطراب المنفرد، الدالة الحدودية، المعلمة الصغيرة، المخطط الامامي.